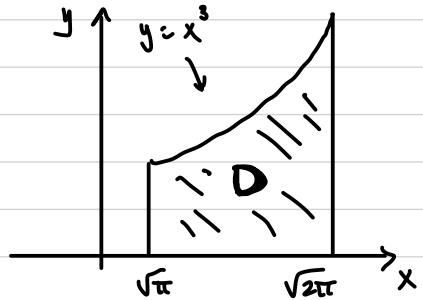


Now, balance ease of describing region with the function being integrated.

Ex $\iint_D \sin\left(\frac{y}{x}\right) dA.$

integrate first
w.r.t. y .



$$= \int_{\sqrt{\pi}}^{\sqrt{2\pi}} \int_0^{x^3} \sin\left(\frac{y}{x}\right) dy dx$$

endpts
of projection

$$= \int_{\sqrt{\pi}}^{\sqrt{2\pi}} -x \cos\left(\frac{y}{x}\right) \Big|_{y=0}^{y=x^3} dx$$

$$= \int_{\sqrt{\pi}}^{\sqrt{2\pi}} -x \cos\left(\frac{x^3}{x}\right) + x dx$$

$$= -\frac{1}{2} \sin(x^2) + \frac{1}{2} x^2 \Big|_{\sqrt{\pi}}^{\sqrt{2\pi}}$$

$$= \frac{2\pi}{2} - \frac{\pi}{2} = \frac{\pi}{2}.$$

$$\begin{aligned} u &= x^2 \\ du &= 2x dx \\ dx &= \frac{du}{2x} \end{aligned}$$

$$\begin{aligned} &\int_{\sqrt{\pi}}^{\sqrt{2\pi}} -\frac{x \cos u}{2x} du \\ &= \int -\frac{1}{2} \cos u du \\ &= -\frac{1}{2} \sin x^2 \end{aligned}$$