

Changing the Order of Integration

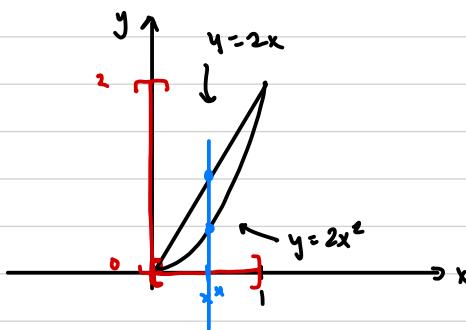
Ex. Change the order of integration of

$$\int_0^2 \int_{\frac{y}{2}}^{\sqrt{\frac{y}{2}}} f(x,y) dx dy.$$

DRAW D.

endpoints

curves



$$\text{outer curve: } x = \sqrt{\frac{y}{2}}$$

$$x^2 = \frac{y}{2} \approx y = 2x^2$$

$$\text{inner curve: } x = \frac{y}{2}$$

$$\int_0^1 \int_{2x^2}^{2x} f(x,y) dy dx$$

$$y = 2x$$

upper curve boundary

lower curve boundary